Abstract

Linear colliders require huge amounts of positrons comparing to ring colliders, because the beam is dumped after the collision. Electron Driven ILC Positron source has been designed as a technical backup of the undulator position source including the beam loading effect, etc. To avoid any damage on target by thermionic and acoustic effects, the positrons are generated in multi-train and multi-bunch format with normal conducting accelerator resulting a high beam current more than 1 A in the initial part of positron linac, the positron capture linac composed from L-band standing wave linac. The beam loading compensation method for the positron capture linac is considered.

INTRODUCTION

ILC is an e+e- linear collider with CME 250 GeV - 1000 TeV [1]. It employs Super-conducting accelerator (SCA) to boost up the beam to the designed energy. The beam is accelerated in a macro pulse with 1300 bunches by 5 Hz repetition. The bunch charge is 3.2 nC resulting the average beam current 21 μA. This is a technical challenge, because the amount of positron per second is more than 40 times larger than that in SLC [2].

In the E-Driven ILC positron source, 3.0 GeV electron beam is the driver for positron generation with 16 mm W-Re alloy target. The configuration is schematically shown in Figure 1. The generated positron is captured and boosted up to 5 GeV by the capture linac and positron booster. ECS (Energy Compressor System) has an important role to improve the efficiency. The 16 mm W-Re target is rotating with 5.0 m/s tangential speed to prevent a potential target damage. FC (Flux Concentrator) generates a strong magnetic field along z direction to compensate the transverse momentum of the positron. 36 1.3 m L-band standing wave accelerators with 0.5 Tesla solenoid field are placed for positron capture. This section is called as Positron Capture Linac. At the downstream of Positron Capture Linac, a chicane is placed to removes electrons. The positron booster is composed from 2.0 m L-and and 2.0 m S-band traveling wave accelerators. ECS is composed from 2.0 m L-band traveling wave accelerators with chicanes.

In E-Driven ILC positron source, the positrons for one pulse (1312 bunches) in main linac are generated in 64 ms. To spread the heat deposition on target on a wider area, the positron is generated in 20 pulses which contains 66 bunches as shown in Figure 2 and the pulse is repeated by 300 Hz in 64 ms with normal conducting accelerator. The heat load on the target is much relaxed with this pulse structure, because only the heat of 66 bunches is accumulated, instead of 1312 bunches [3]. The pulse format shown in Figure 2 is identical to a part of the DR fill pattern. Depending on the DR fill pattern [4], the beam structure is should be matched.

A first simulation for the injector part is made by T. Omori [3]. A simulation with the tracking down to DR was made by Y. Seimiya [5], but no beam loading effect was accounted. A new simulation with the beam-loading effect was done by Kuriki and Nagoshi [6] giving the peak energy deposition density less than the practical limit, 35 J/g [7].

The generated positron has a large spread in both longitudinal and transverse momentum space. Capturing the positron in an RF bucket for further acceleration is an important issue. Historically, the acceleration capture has been pursued. The generated positrons are placed on acceleration phase of RF cavity to suppress the momentum spread adiabatically, but this method has some limitation because only positrons in a good phase space are captured and others are lost. Deceleration capture was proposed by M. James et al. [8] for better capture efficiency. In this method, the
positrons are placed on a deceleration phase and move to the acceleration phase by phase-slipping. As the intermediate state, the positron phase space distribution is large in longitudinal momentum, but small in RF phase (φ). By boosting the positrons further, the longitudinal momentum spread is suppressed resulting a good capture efficiency.

This deceleration capture cause a difficulty on the beam loading compensation. We discuss this issue in this article.

**POSITRON CAPTURE LINAC**

We explain the positron capture linac in this section. For other systems, please refer Ref. [9]. For the positron capture linac, we employ the standing wave L-band structure developed for the undulator positron source [10]. The advantage of this structure is a wide aperture, 60 mm in 2a resulting a better positron capture. The accelerator is surrounded by solenoid magnet to provide 0.5 Tesla magnetic field along the accelerator for focusing.

One RF unit is composed from two L-band klystrons and four accelerators. The power of the klystron is 50 MW. Accounting 10% WG loss, the effective input power for one accelerator is 22.5 MW. In the capture linac, the beam loading current is dynamically varied by bunching and particle loss. It is up to 1.6 A [9]. In the simulation, the accelerator voltage is determined according to the beam loading current for each cavity [9]. The acceleration voltage per structure is between 12 - 20 MV.

According to the simulation, the configuration is determined as 9 units (18 klystrons and 36 accelerators). One unit length is 6.00 m giving the total length of the capture linac is 54 m.

In the simulation, both positrons and electrons were accounted. The accelerating field of the structure is determined by the input power (22.5 MW per structure) and the beam loading current. The beam loading current is a vector sum of each particle accounting the charge and RF phase. The beam loading current is calculated from the previous simulation used as the input to the next iteration. Figure 3 shows the beam loading current obtained from each iteration is plotted.

where β is a coupling, \( P_0[W] \) is the peak input power, \( r[\Omega/m] \) is shunt impedance, \( L[m] \) is the structure length, \( I[A] \) is beam current, \( t_b \) is timing when the beam pulse starts, and \( T_0 \) is a time constant given as

\[
T_0 = \frac{2Q}{\omega(1 + \beta)}
\]

determined with \( Q \) and \( \omega \). The first term of Eq. (1) is RF term and the second term is the voltage induced by the beam (Beam loading). These two terms have the same time constant, the accelerating voltage can be constant during the acceleration with a proper condition. If we differentiate Eq. (1) with \( t \),

\[
\frac{\partial V}{\partial t} = 2 \sqrt{\beta P_0 r L} \frac{1}{1 + \beta} e^{-\frac{t_b}{T_0}} - \frac{r L I}{1 + \beta} e^{-\frac{t-b}{T_0}},
\]

is obtained. It becomes zero if

\[
t_b = T_0 \ln \left( \frac{1}{2} \frac{r L}{\beta P_0} \right).
\]

If this condition is satisfied, the acceleration voltage is flat during the acceleration. The voltage \( V \) is

\[
V = \frac{2 \sqrt{\beta P_0 r L}}{1 + \beta} \left( 1 - \frac{1}{2} \frac{r L}{\beta P_0} \right).
\]

This is a conventional way to compensate the beam loading effect in a standing wave. This is applicable as long as the beam is accelerated on the crest, i.e. zero phase. If the beam in off crest, Eq. (1) becomes

\[
V(t) = \frac{2 \sqrt{\beta P_0 r L}}{1 + \beta} \left( 1 - e^{-\frac{t}{T_0}} \right) \cos(\omega_0 t + \phi_0) - \frac{r L I}{1 + \beta} \left( 1 - e^{-\frac{t-b}{T_0}} \right) \cos(\omega_0 t + \theta + \phi_0),
\]

where \( \omega_0 \) is angular frequency of 1.3 GHz, \( \phi_0 \) is initial phase, and \( \theta \) is the beam phase with respect to the RF phase. In this case, a constant RF amplitude can’t be made by adjusting the amplitude. RF amplitude and phase (sum of input RF and beam) are varied over the pulse. The capture efficiency is also varied resulting a large variation of positron intensity.

In the deceleration capture, the positron is placed on a deceleration phase and captured in an acceleration phase. The positron phase is then moving from the deceleration phase...
to the acceleration phase by phase slipping. The positron is always sitting on off crest phase. The phase effect on the beam loading compensation should be accounted.

To revive the beam loading compensation, we introduce a detuning angle, $\psi$. Detuning angle is defined as

$$\psi \equiv \tan^{-1}\left(\frac{\Delta \omega}{\omega_0}\right),$$

where $\Delta \omega$ is the detuning angular frequency of the cavity.

In this case, the cavity induced voltage $V_c$ has a phase shifted from input RF phase with $\psi$ as shown in Figure 4. If the beam is placed at the same phase to the input RF, the power by the beam loading is in opposite phase as shown in Figure 4, because the minus sign of the beam loading. The induced voltage by the beam loading $V_{BL}$ has angle $\psi$ from the beam loading power as shown in the figure with a dotted-dash line. As a result, the induced voltage by RF $V_{RF}$ and beam loading $V_{BL}$ are in opposite phase (π) and the beam loading compensation by Eq. (6) is revived.

![Figure 4: Phase diagram of cavity voltage with a detuning angle. Input RF is defined as zero phase shown with a dashed line arrow. The induced voltage by RF ($V_{RF}$) has an angle $\psi$ from the input RF shown with a solid line. The beam loading input is opposite phase to the input RF. The induced voltage by Beam loading $V_{BL}$ has an angle $\psi$ from the beam loading input.](image)

The effective acceleration phase to the beam is $\psi$ in this case. Therefore, the acceleration phase should be adjusted by the detuning. Because setting plungers for each cavity is not realistic, the frequency should be adjusted by temperature. If we assume $\psi = \pi/4$, required detuning on the frequency is

$$\frac{\Delta \omega}{\omega_0} = \tan \psi \frac{1}{2Q},$$

giving $1.7 \times 10^{-5}$ with $Q = 29700$ [10]. By using thermal expansion coefficient of copper, $16.8 \times 10^{-6}/\text{K}$, the equivalent temperature of the detuning is 1.0 K. A typical accuracy of the temperature control of RF cavity is 0.1 K which corresponds to the phase resolution of 0.08 rad. The amplitude error by the phase fluctuation $\Delta \psi$ is

$$\cos(\psi + \Delta \psi) \sim \cos \psi - \sin \psi \sin \Delta \psi,$$

(9)

It is negligible for small $\psi$, but could be significant for large $\psi$. The effect should be evaluated with a simulation, but it could be a next issue.

**SUMMARY**

We consider the beam loading compensation for the positron capture linac for ILC E-Driven positron source. Due to the heavy beam loading, its compensation should be implemented. The conventional way for the compensation by adjusting the amplitude does not work properly, because the beam loading phase is dynamically varied in the deceleration capture method. We consider the beam loading compensation with the detuning angle. In this method, the beam is placed always on the same phase as the RF phase. The RF induced voltage and beam induced voltage are exactly same phase (opposite phase). In this case, the beam loading compensation works well as expected. The phase of the cavity RF felt by the beam is controlled by the detuning angle. To vary the phase $\pm \pi/4$, the temperature should be consolved $\pm 1.0$ K. The phase accuracy is 0.08 rad assuming 0.1 K temperature stability. The effect of the temperature stability should be confirmed by a simulation.

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**REFERENCES**